

**11.14**

From the block diagram, the characteristic equation is obtained as

$$1 + K_c \left[ \frac{(0.5) \left( \frac{4}{s+3} \right)}{1 + (0.5) \left( \frac{4}{s+3} \right)} \right] \left[ \frac{2}{s-1} \right] \left[ \frac{1}{s+10} \right] = 0$$

that is,

$$1 + K_c \left[ \frac{2}{s+5} \right] \left[ \frac{2}{s-1} \right] \left[ \frac{1}{s+10} \right] = 0$$

Simplifying,

$$s^3 + 14s^2 + 35s + (4K_c - 50) = 0$$

The Routh Array is

$$\begin{array}{cc} 1 & 35 \\ 14 & 4K_c - 50 \\ \frac{490 - (4K_c - 50)}{14} & \\ 4K_c - 50 & \end{array}$$

For the system to be stable,

$$\frac{490 - (4K_c - 50)}{14} > 0 \quad \text{or} \quad K_c < 135$$

$$\text{and } 4K_c - 50 > 0 \quad \text{or} \quad K_c > 12.5$$

Therefore  $12.5 < K_c < 135$